

# Implementing with veto players: simple mechanisms

J. Arin\* and V. Feltkamp<sup>†</sup>

September 1, 2004

## 1 Introduction

In 1997, Dagan, Serrano and Volij present a simple tree games for bankruptcy problems. In the game a special player, the one with highest claim, has a special role. He is the proposer and the rest of the players answer to this proposal. In the case of a negative answer the conflict is solved bilaterally, applying a normative solution concept to a special two-claimant bankruptcy problem. This paper studies similar simple tree games in the context of coalitional games with a veto player. The veto player is the proposer and similarly to the case of Dagan, Serrano and Volij in the case of negative answer of some player a bilateral resolution is formulated.

The paper shows that with this simple mechanisms the outcomes of any Nash equilibrium should belong to a certain set. And those outcomes are not necessarily efficient. The second part of the paper studies a more complex tree game where the veto player, the proposer, could make sequential proposals whenever there is a positive value to divide among the players.

---

\*Dpto. Ftos. A. Económico, University of the Basque Country, L. Agirre etorbidea 83, 48015 Bilbao, Spain. Email: jeparagj@bs.ehu.es. This author thanks financial support provided by the Project 9/UPV00031.321-15352/2003 of The Basque Country University and the Project BEC2003-08182 of the Ministry of Education and Science of Spain.

<sup>†</sup>School of Management, PO Box 1203, 6201 BE Maastricht, The Netherlands.

## 2 The model

Given a veto balanced game  $(N, v)$ , we will define a tree game associated to the TU game and denoted by  $G(N, v)$ . The game has  $n$  stages and in each stage only one player is playing. In the first stage a veto player is playing and he announces a proposal  $x^1$  that belongs to the set of feasible and non negative allocations of the game  $(N, v)$ . In the next stages the non veto players are playing, each one once at one stage. They have two actions. To accept or to reject. If a player, let say  $i$ , accepts the proposal  $x^{t-1}$  at stage  $t$ , he leaves the game with the payoff  $x_i^{t-1}$  and for the next stage the proposal  $x^t$  coincides with the proposal at  $t - 1$ , that is  $x^{t-1}$ . If player  $i$  rejects the proposal then a two-person TU game is formed with the veto player and the player  $i$ . In this two-person game the value of the grand coalition is  $x_1^{t-1} + x_i^{t-1}$  and the value of the singletons is obtained by applying the Davis-Maschler reduced game given the game  $(N, v)$  and the allocation  $x^{t-1}$ . The player  $i$  will receive as payoff the result of some restricted standard solution applied in the two-person game.

*Input* : a veto-rich game  $(N, v)$  with a veto player, the player 1, and an order in the set of the rest players (responders)

*Output* : a feasible and non negative distribution  $x$ .

1. Start with stage 1. The veto player makes a feasible and not negative proposal  $x^1$  (not necessarily an imputation).
2. Let the stage  $t$  where the  $t$  responder plays, given the allocation  $x^{t-1}$ . If he says yes he receives the payoff  $x_t^{t-1}$ , leaves the game, and  $x^t = x^{t-1}$ . If he says no he will receive the payoff

$$y_t = \max \{0, 1/2(x_1^{t-1} + x_t^{t-1} - v_{x^{t-1}}(\{1\}))\} \text{ where}$$

$$v_{x^{t-1}}(\{1\}) = 1 \in S \subseteq N \setminus \{t\} \max \{v(S) - x^{t-1}(S \setminus \{1\})\}$$

$$\text{Now, } x^t = \begin{cases} x_1^{t-1} + x_2^{t-1} - y_t & \text{for player 1} \\ y_t & \text{for player } t \\ x_i^{t-1} & \text{if } i \neq 1, 2 \end{cases}$$

3. The game ends when the stage  $n$  is played and we define  $x^n(N, v)$  as the vector with coordinates  $(x_j^n)_{j \in N}$ .